## Fiscal Policies: Taxes

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Fiscal Policies: Taxes

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## Question

#### • What is the government's main duty?

- Governance
  - Regulation
  - Protect Property right
- Provide Public goods
- Internalize Externalities
- Antitrust
- Redistribution
- Stabilization
- . . . .
- Market Failure
- Government Failure

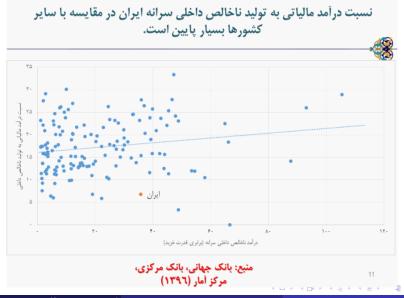
- Ramsey Government: Optimum Aggregate Welfare
- Mirrlees Government: Optimum Socially Welfare
  - Maxiizing a social optimum function which is a weighted average of HHs' welfare.

- Taxes (Corporate taxes, Value-added tax, Personal Income, Social Security Taxe, Excise Tax, Import Taxes)
- Debts
- Money (Seigniorage)
- Natural Resources Income like Oil Income or ...
- Selling Assets



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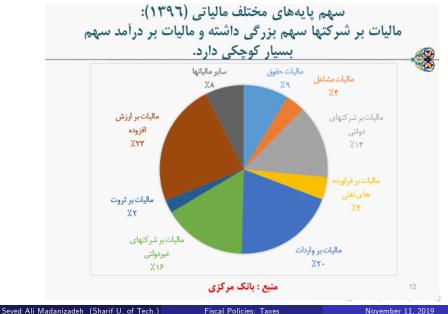
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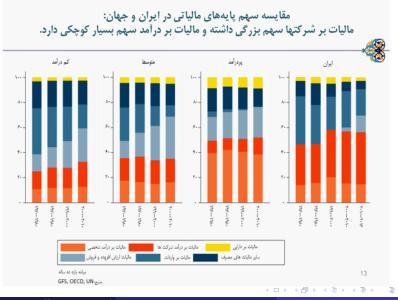


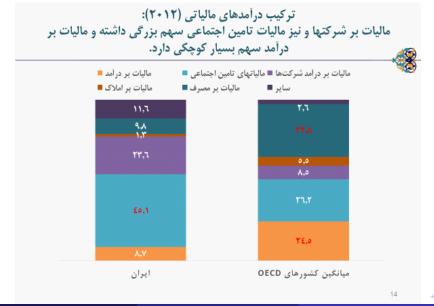
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- A simple model
  - Household
  - Production
  - Government
- Types of taxes
  - Labor income Tax
  - Capital Income Tax
  - Consumption Tax
  - Natural Resources Lump-sum Tax

• Government Expenditures = G = T =Taxes

• 
$$c_g = \phi \left( G - S' 
ight)$$
 where  $\phi \leq 1$ :

- S' is the subsidy transfers from government
- c<sub>g</sub> could be public or private goods that government produces with some level of efficiencies, usually less that one (mostly close to zero;))
- Explanations of  $c_g$  and S
  - What does Government actually do
    - When it receives taxes?
    - When it produces a public (or private) good?
    - When it redistributes the taxes?

### Model: Labor Income Tax

• Firm problem:

$$Y = AH$$

• Household Problem

$$\max_{\substack{c,h}} U\left(c_{p}, c_{g}, h\right)$$
 s.t.  $c_{p} = (1 - \tau) wh + S'$ 

where t is the tax rate and S' is the subsidy transfers from government

• Example:

$$\max_{c,h} 2\sqrt{c_p + c_g} - h$$
  
s.t.  $c_p = (1 - \tau) wh + S'$ 

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• Equivalent problem

$$\max_{c,h} 2\sqrt{C} - h$$
  
s.t.  $C = (1 - \tau) wh + S$ 

where  $S = S' + c_g$ 

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#### • HH's Solution

$$h = (1 - \tau) w - \frac{S}{(1 - \tau) w}$$
  
$$c = (1 - \tau)^2 w^2$$

• Firm's solution:

$$w = A$$

### Model: Labor Income Tax

• Suppose  $S'=0 \Rightarrow S=c_g=\phi G=\phi au wh$ 

• Equilibrium

$$h = \left(\frac{1-\tau}{1-\tau+\phi\tau}\right)(1-\tau)A$$

$$G = \left(\frac{1-\tau}{1-\tau+\phi\tau}\right)(1-\tau)\tau A^{2}$$

$$C = (1-\tau)^{2}A^{2}$$

$$C_{p} = (1-\tau)^{2}A^{2}\left(\frac{1-\tau}{1-\tau+\phi\tau}\right)$$

$$Y = \left(\frac{1-\tau}{1-\tau+\phi\tau}\right)(1-\tau)A^{2}$$

$$Welfare = \left(\frac{1-\tau+2\phi\tau}{1-\tau+\phi\tau}\right)A(1-\tau)$$

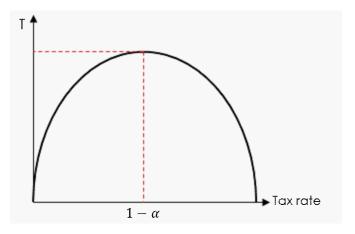
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### Model: Labor Income Tax

• Laffer Curve

$$G = T = au \left( 1 - au 
ight) A^2$$



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• Production:

$$Y = AK^{\alpha}$$

• Household $\max_{\substack{c_t,k_{t+1}\\t=0}}\sum_{t=0}^{\infty}\beta^t U(c_t)$ s.t.  $c_t + k_{t+1} - (1-\delta) k_t = (1-\tau) [v_t k_t + \pi_t]$ • Government

$$G_t = T_t = \tau \left( v_t k_t + \pi_t \right)$$

• Solution:  $\frac{u_{ct}}{u_{ct+1}} = \beta \left(1 - \delta + (1 - \tau) v_{t+1}\right)$ 

• Firm:

$$\pi_t = Y_t - v_t k_t$$
$$v_t = \alpha A K_t^{\alpha - 1}$$

• Government: Assume  $\phi = 0$ 

• Steady State Equilibrium

$$1 = \frac{1}{1+\rho} \left(1-\delta + (1-\tau) \alpha A K_{ss}^{\alpha-1}\right)$$

$$K_{ss} = \left(\frac{\alpha}{\rho+\delta} (1-\tau)\right)^{\frac{1}{1-\alpha}} = K_0 (1-\tau)^{\frac{1}{1-\alpha}}$$

$$Y = A \left(\frac{\alpha}{\rho+\delta} (1-\tau)\right)^{\frac{\alpha}{1-\alpha}} = Y_0 (1-\tau)^{\frac{\alpha}{1-\alpha}}$$

$$I_{ss} = \delta K_{ss}$$

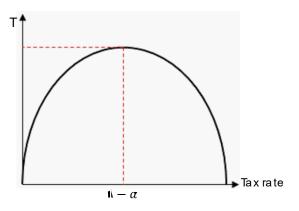
$$C_{ss} = (1-\tau) A K_{ss}^{\alpha} - \delta K_{ss} = C_0 (1-\tau)^{\frac{1}{1-\alpha}}$$

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# Model: Capital Income Tax

• Laffer Curve:

$$G_{ss} = T_{ss} = K_0^{lpha} \tau \left(1 - \tau\right)^{rac{lpha}{1-lpha}}$$



• Production:

$$Y = AK^{\alpha}L^{1-\alpha}$$

Household

$$\max_{c_t,k_{t+1}}\sum_{t=0}^{\infty}\beta^t U(c_t,I_t)$$

s.t.  $c_t + k_{t+1} - (1 - \delta) k_t = (1 - \tau_{lt}) w_t l_t + (1 - \tau_{kt}) (v_t k_t) + \pi_t$ 

Government

$$G_t = T_t = \tau_{lt} w_t l_t + \tau_{kt} \left( v_t k_t + \pi_t \right)$$

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• Optimum  $\tau_{kt}$ ,  $\tau_{lt}$  : Solution:

$$egin{array}{rcl} au_{kt} &=& 0 ext{ for } t \geq 1 \ au_{lt} &=& ar au_l ext{ for } t \geq 0 \end{array}$$

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• For each G :there is a tax rate  $\tau\left(G\right)$  to finance G and also  $\mathit{C_g}=\phi G$  • HH Welfare

$$U\left(\mathcal{C}_{g},\mathcal{C}_{p}^{*}\left( au
ight),I^{*}\left( au
ight)
ight)$$

• Government problem: Choose G s.t.

$$\max_{G} W\left(\phi_{G}, \tau\left(G\right)\right)$$

- Distortion and productivity Effect
- Crowding out Consumption
- Crowding out Investment
- Fiscal Multiplier