

# Monetary Economics

## Inventory Model

Seyed Ali Madanizadeh

Sharif University of Technology

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# Monetary Economics

- Money Neutrality
  - Short run
  - Long run
- Schools of thoughts
- Modeling
  - Money Demand
  - Money Supply
    - Money aggregates
    - Interest rate targets
  - Equilibrium
    - Frictionless economies
    - Frictional economies

# Demand for Money

- Why do people hold money?
- People hold money to facilitate transactions.
- There are costs to holding money: foregone interest, risk of theft, etc.
- What is the optimal level of money holdings? i.e. how is money demand determined?

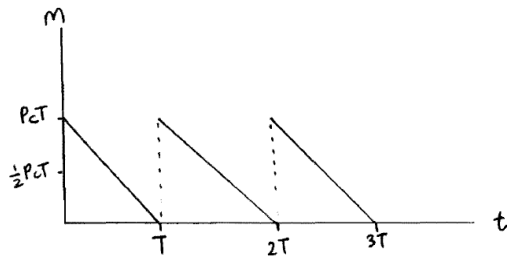
# Demand for Money

- Money Demand Models
  - Inventory Theory: Baumol Tobin model
  - Money in Utility
  - Cash in advance model
  - Transaction technology
  - Search models

# Inventory Model: A Simple Model of Optimal Cash Management

- Consumer's problem:
  - They make consumption purchases totalling  $p * c$  every year and these have to be made in **cash**
- Purchases are spread evenly throughout every day of the year (For simplicity)
- There is a nominal cost of going to the bank/ATM to get money,  $\$ \gamma$
- Deposits in the bank earn interest,  $R$ .
- The consumer goes to the bank at regular intervals, every  $T$  years (For simplicity).
  - ex: If  $T = \frac{1}{12}$  , he/she goes every month
  - Frequency = # of bank visits per year =  $\frac{1}{T}$

# Inventory Model



# Inventory Model

- What is optimal  $T$ ?
- The consumer will want to minimize costs and also have enough cash at hand for consumption.
- Costs:
  - i) bank visits =  $\$ \gamma$  per visit.
  - ii) foregone interest:  $R$

# Inventory Model

- i) Bank visits (transaction cost): Annual (nominal) cost of bank visits =  $\gamma * \frac{1}{T}$

- Annual (real) cost of bank visits =

$$\frac{\gamma}{p} * \frac{1}{T}$$

(Used to be called "shoe leather costs")



# Inventory Model

- Foregone interest:
  - In each visit, consumer wants to take out just enough cash to cover expenditures until next visit.
  - Why? Because by holding too much cash, you lose interest.
  - Then the question is: how much will the consumer spend between each trip?
  - Recall: We assumed that purchases are spread evenly through every day of the year.

# Inventory Model

- Total amount spent between trips =

$$p * c * T$$

So, you withdraw  $pcT$  every time you visit.

- So, is foregone interest =  $pcTR$ ?

# Inventory Model

- NO! Because you don't hold all this money that you withdraw for the entire period, you spend it down evenly.
- Average money holdings = half the distance to the peak.

$$m = \frac{1}{2}pcT$$

- Average money holdings =

$$\frac{m}{p} = \frac{1}{2}cT$$

- Avg. real interest foregone =

$$\frac{1}{2}cTR$$

# Inventory Model

- Intuition: As  $T \uparrow$ , you go to the bank every  $T$  years, so less often.
  - As  $T \uparrow$ , transaction costs  $\downarrow$
  - As  $T \uparrow$ , avg. money holdings  $\uparrow \Rightarrow$  foregone interest costs  $\uparrow$  (bec. you withdraw more in each visit).

# Inventory Model

- Optimal  $T$  :
  - minimize the total cost:

$$\min_T TRC = \frac{\gamma}{p} * \frac{1}{T} + \frac{1}{2}cTR$$

- FOC  $\Rightarrow$

$$T^* = \sqrt{\frac{2\gamma}{pcR}}$$

# Inventory Model

- Implications: You go less often (i.e.  $T \uparrow$ ) when
  - Transaction costs,  $\gamma \uparrow$
  - Nominal consumption,  $pc \downarrow$
  - Interest rate,  $R \downarrow$

# Inventory Model

- Money Demand:
  - Given  $T$ , let's calculate avg. money holdings

$$\begin{aligned}\frac{m}{p} &= \frac{1}{2}cT^* \\ &= \sqrt{\frac{c\gamma}{2pR}}\end{aligned}$$

# Inventory Model

- Let  $\gamma_{\text{real}} \equiv \frac{\gamma}{p}$
- Aggregate real money demand (rela money balances):

$$\begin{aligned}\frac{M}{P} &= \sqrt{\frac{c\gamma_{\text{real}}}{2R}} \\ &= \Phi(C, R, \gamma_{\text{real}}) \\ &\quad (+, -, +)\end{aligned}$$

- Financial Innovation goes up:  $\downarrow (\gamma_{\text{real}}) \Rightarrow \frac{M}{P} \downarrow$



# Inventory Model

- Define  $\bar{\gamma}_{\text{real}} = \frac{\gamma}{p c}$  (real  $\gamma$  relative to total consumption (or production))
- Compare to Equation of Exchange

$$\text{Velocity} = v = \sqrt{\frac{2R}{\bar{\gamma}_{\text{real}}}}$$

⇒ Quantity Theory of Money

$$Mv = PY$$

# Inventory Model

- Supply and Demand of Money

$$M^s = P\Phi(Y, R, \gamma_{\text{real}})$$

- Long run: Flexible prices
  - $M$  determines  $P$
- Short run: Sticky prices!
  - $M$  determines  $Y, R$